1. INTRODUCTION

For decades, the concept of a bit has been the fundamental unit for information encoding in computer science. Recent advances in quantum computing have led to the first commercial quantum computers which operate on quantum bits (qubits) instead of bits [National Academies of Sciences, Engineering and Medicine 2019]. Analogous to a bit that can be either 0 or 1, a qubit can also take one of two states: |0⟩ and |1⟩. But in addition, due to quantum mechanics, it can also be in a combination of these two states at once - a superposition of states. Empowered by superposition and other fundamental properties of quantum mechanics, quantum computers have the potential to solve certain problems faster than conventional computers [Horodecki et al. 2009]. In fact, various algorithms for quantum computers exist for which a theoretical linear or exponential speed-up over their classical counterparts was demonstrated, e.g. for the factorization of prime numbers [Shor 1999].

As the number of available qubits of quantum computers increases, more companies start to explore quantum computing. However, it is expected that near-term devices will only contain up to a few hundred qubits [Preskill 2018]. Another restricting factor is that these qubits are not perfect: Their states are only stable for a short amount of time. Because of their rapid decay, only a limited number of operations can be executed on them. Thus, successfully programming quantum computers today is limited by the available hardware.
Besides, the shear fact that quantum computers obey the law of quantum mechanics results in - from the point of a software developer - unusual effects. To illustrate how different quantum computing is, we describe implications for two basic programming tasks: reading, and loading data. For the first task of reading a qubit, its quantum state must be accessed. This can only be done by measuring it. Unfortunately, measurement causes a qubit to collapse to either $|0\rangle$ and $|1\rangle$. Thus, the state of a qubit that is in superposition cannot be accessed for reading.

The second task consists of loading data into a quantum computer. This task is at the beginning of almost every algorithm that processes input data. After the initial loading process, the data is represented by qubits via a specific encoding. Each algorithm expects that a certain data encoding is used, and then processes the data by performing calculations. Unfortunately, loading data can not always be done efficiently. In the worst case, loading requires exponential time. This slows down algorithms with an otherwise logarithmic or linear runtime: With an exponential loading time, their overall runtime is also exponential. This ruins a theoretical linear or exponential speedup of an algorithm - which was one of the reasons why we wanted to use a quantum computer in the first place. In general, the time for loading depends (i) on the routine that loads the data in a specific encoding and (ii) on the data itself. Thus, loading data is not a trivial task that influences the runtime complexity of a quantum algorithm.

To help software developers understand the implications of using a specific encoding to load data, we formulate three common data encodings as patterns. A pattern in the spirit of Alexander et al. [1977] describes a proven solution to a re-occurring problem. For the development of software, documenting patterns is commonly used to capture knowledge about a specific domain [Coplien 1996] [Buschmann et al. 1996]. Especially in an interdisciplinary and complex domain like quantum computing, patterns can be used to make proven solutions explicit, explain ‘how’ they work, and ‘why’ a solution (e.g. an encoding) should be used [Meszaros and Doble 1997].

The remainder of this paper is structured as follows: Section 2 describes fundamentals of quantum computing. Section 3 starts with an overview of patterns for quantum algorithms and then presents the new encoding patterns. Related work is discussed in Section 4. Finally, Section 5 concludes the paper and describes future work.

2. FUNDAMENTALS OF QUANTUM COMPUTING

The core concept of quantum computing is the qubit. In this section, we will briefly define qubits and their basic properties that can be used to encode data. Mathematically, the state $|\psi\rangle$ of a qubit is defined as follows:

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle = \alpha|0\rangle + \beta|1\rangle$$

In the equation above, we use the Dirac notation that represents a vector $v$ as $|v\rangle$. The two orthogonal basis vectors $\{|0\rangle, |1\rangle\}$ span up a two-dimensional vector space and are also referred to as computational basis. The complex numbers $\alpha$ and $\beta$ are called amplitudes: With a probability of $|\alpha|^2$, measuring the qubit in the computational basis results in the $|0\rangle$ state. Analogously, the qubit can be measured as $|1\rangle$ with a probability of $|\beta|^2$. As these are the only two possible outcomes of the measurement, their probabilities must sum up to 1. For $\alpha, \beta \neq 0$, the state of a qubit is in superposition: a linear combination of $|0\rangle$ and $|1\rangle$.

While the previous equations describes the state of a single qubit, the state of multiple qubits in a quantum computer (a quantum register) can be described in a similar manner. For example, the two qubits $|\psi_1\rangle$ and $|\psi_2\rangle$ can form a 2-qubit quantum register. If both qubits are in state $|0\rangle$, then the state of the register can be written as $|00\rangle$. As each qubit can be $|0\rangle$, $|1\rangle$, or in a superposition, the 2-qubit register can be in the states $|00\rangle$, $|01\rangle$, $|10\rangle$ or $|11\rangle$, or in a superposition of them [Gruska 1999]:

$$|\psi_1\psi_2\rangle = \alpha_0|00\rangle + \alpha_1|01\rangle + \alpha_2|10\rangle + \alpha_3|11\rangle , \text{ where } \sum_{i=0}^{3} |\alpha_i|^2 = 1. \quad (2)$$

Sometimes the bit strings are transformed into decimal representations resulting in natural numbers, thus, the state vectors are written even more compact as $|0\rangle$, $|1\rangle$, $|2\rangle$, and $|3\rangle$. 

Data Encoding Patterns for Quantum Computing — Page 2
In this work, we focus on gate-based quantum computers for which operations on qubits can be done by applying quantum gates. Quantum gates are defined as matrices and their application to one or multiple qubits results in a state that can be calculated by multiplying the matrix with the state vector. For example, applying the $X$ gate (which is defined by the matrix $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$) to a qubit in state $|0\rangle$, changes its state to $|1\rangle$:

$$X |0\rangle = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$ (3)

Vice versa, applying the $X$ gate to a $|1\rangle$ state leads to the $|0\rangle$ state. In classical computers, this gate corresponds to a NOT gate that flips the state of a bit. Unlike their classical counterparts, the application of a quantum gate can also result in superposition, e.g., applying the so-called Hadamard gate to a qubit in state $|0\rangle$, leads to an equal superposition of both $|0\rangle$ and $|1\rangle$:

$$H |0\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & -1 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \frac{1}{\sqrt{2}} |0\rangle + \frac{1}{\sqrt{2}} |1\rangle$$ (4)

The qubit is measured as $|0\rangle$ and $|1\rangle$ with a probability of $\left(\frac{1}{\sqrt{2}}\right)^2 = 0.5$. For more examples of quantum gates and an in-depth introduction to their mathematical foundation, we refer to [Nielsen and Chuang 2010].

3. PATTERNS FOR QUANTUM ALGORITHMS

In this section, we first introduce quantum algorithms and give an overview of patterns for quantum computing. This includes existing patterns for quantum algorithms that were introduced by [Leymann 2019] as well as the new encoding patterns. We then describe our pattern format and introduce the new encoding patterns. An excerpt from the encoding patterns can also be found on our website [http://quantumcomputingpatterns.org].

3.1 Overview of Patterns for Quantum Algorithms

Fig. 1 presents an overview of patterns for quantum algorithms [Leymann 2019] and the new encoding patterns marked in bold. Due to space limitations, QRAM and ANGLE ENCODING are not described further in this paper. The figure also illustrates the typical steps of a hybrid quantum algorithm [Leymann et al. 2020]: Some steps are executed on a classical computer (light background), others on a quantum computer (dark background).

First, data is pre-processed on a classical computer. This step is required for some data encodings or algorithms. In the next step, data is loaded into a quantum computer: All qubits are initialized as $|0\rangle$, so the overall quantum state can be denoted as $|00\ldots0\rangle$. A state preparation routine operates on a register of qubits and thus, changes their state. As a result, a quantum state is prepared that represents the data via a specific data encoding. This state can have certain characteristics of quantum states that are described by patterns of the quantum states category. For example, in a UNIFORM SUPERPOSITION, all possible outcomes of the quantum register are equally likely. After the state is prepared, the data is loaded. This overall process of preparing the state is summarized in the INITIALIZATION pattern [Leymann 2019] - another alias for it is State Preparation.

After state preparation, the quantum computer performs computations on the quantum register. These computations are unitary transformations and are represented as quantum gates. Patterns of the category Unitary Transformations describe best practices to construct computations that happen in this step. For example, UNCOMPUTE can be used to reset the state of a quantum register to the ground state $|00\ldots0\rangle$.

In the last step that is executed on the quantum computer, one or multiple qubits are measured. The measurement results are analyzed in an optional post-processing step. Depending on the results or overall goals of the algorithm, the algorithm terminates or proceeds with the next iteration in the pre-processing step. Program flow patterns capture higher-level strategies to solve a problem on a quantum computer.
3.2 Pattern Format and Method

Pattern authors make use of different pattern formats [Coplien 1996] that define the sections of their pattern documents. We use an existing pattern format of Fehling et al. [2014] and extend it by additional sections for aliases and forces of the pattern. Each pattern is introduced by a descriptive Name that is followed by a graphical Icon. Next to the icon, we denoted the Intent of the pattern: a short sentence that summarizes the pattern. Optionally, other names under which a pattern may be known are listed in the Alias section. In the Context section, we describe the circumstances that lead to the problem and preconditions for applying the pattern. Considerations and trade-offs that must be taken into account when solving the problem are described in the Forces section. The Solution is a high-level description of how to solve this problem and is further illustrated in the Solution Sketch. The Result of the solution discusses the consequences of using this pattern, e.g. the new context that results. If aspects of this pattern can be varied, this is covered in Variants. Relations to other quantum computing patterns are described in the Related Patterns. Finally, Known Uses of the pattern are listed, which is either a concrete implementation of the pattern or a published quantum algorithm that uses this pattern.

In Section 3.1, we explained that a state preparation routine is used to realize the encoding of data. Therefore, the solution section of our patterns describes (i) how the data is represented, and (ii) the process of encoding data via a suitable state preparation routine. If various state preparation routines can be used to realize one particular encoding, they are referred to in the Known Uses section. In this section, we also name concrete examples of algorithms that require this particular data encoding.

Patterns are not invented but abstracted from real-world solutions [Kohls 2010]. In quantum computing, algorithms for quantum computers have been published for decades before the first quantum computer was realized. Concrete software implementations therefore often refer to a quantum algorithm that is described in a scientific publication. These publications also contain the underlying idea of the algorithm - the abstract solution that we want to capture in a pattern. In contrast to that, typical software patterns are abstracted only from existing implementations [Fehling et al. 2014, Fehling et al. 2015]. For our pattern research, we followed the method described by [Fehling et al. 2014]. To identify patterns in the domain of quantum algorithms, we analyzed research papers, books, and technical documentation. During this phase, we collected reoccurring solutions and pattern ideas. If we identified at least three references per pattern idea (Coplien's Rule of Three [Coplien 1996]), we abstracted the underlying solution from the references and authored a pattern.
3.3 Data Encoding Patterns

In this section, we present data encoding patterns for quantum algorithms. Each pattern describes how input data is loaded in a specific encoding at the beginning of a quantum algorithm. Because data is loaded during the \textsc{Initialization} step (see Fig. 1), each encoding pattern further refines this pattern. Therefore, we start by giving a short summary of \textsc{Initialization} [Leymann 2019] and then extend the original pattern by a detailed description of the forces. As these are also the forces of the new encoding patterns, we omit this section in the encoding patterns.

We first present the simplest encoding, \textsc{Basis Encoding}, and then introduce \textsc{QuAM} (\textsc{Quantum Associative Memory}), and \textsc{Amplitude Encoding}. Historically, solving quantum physical problems was in the foreground of quantum computing, thus, input data for quantum algorithms is often numeric. Therefore, we assume in the context of each pattern that the input data $X$ is numeric.

\textbf{Initialization}

\begin{itemize}
  \item \textbf{Summary:} At the beginning of an algorithm, its initial state is prepared: First, the registers are initialized in the \ket{0...0} state. If input data is used by the algorithm, a suitable state preparation routine encodes the data via a specific encoding.
\end{itemize}

\textbf{Forces.} Encoding data in qubits is not trivial. Current devices contain a limited amount of qubits that are stable for a short amount of time. In order to make use of current devices, the representation must be compact and use only a few qubits and few quantum gates. Because qubits decay fast and quantum gates are error-prone too, the number of operations to prepare the quantum state must be small. To encode even a large number of data values efficiently, a logarithmic or linear runtime is ideal, i.e., the state preparation routine consists of a logarithmic or linear number of parallel operations. Each encoding is essentially a trade-off between two major forces: (i) the number of required qubits and (ii) the runtime complexity for the loading process. Besides that, an additional force requires that data must be represented in a suitable format for further operations. For arithmetic operations like addition or multiplication often the exact values of the data need to be represented. For other operations it may be sufficient to represent their relative values (e.g., as relatively small or large amplitude of a quantum state with \textsc{Amplitude Encoding}).

\textbf{Basis Encoding}

\begin{itemize}
  \item \textbf{Represent a data element in a quantum computer in order to perform calculations}
  \item \textbf{Context.} A quantum algorithm requires numerical input data $X$ for further calculations.
  \item \textbf{Solution.} The main idea for this encoding is to use the \textit{computational basis} $\{\ket{00...0}, \ket{00...01}, \ldots, \ket{11111}\}$ to encode the input data: An input number $x$ is approximated by a binary format $x := b_{n-1} \ldots b_1 b_0$ which is then turned into the corresponding basis vector $\ket{x} := \ket{b_{n-1} \ldots b_1 b_0}$. For example, the number “2” is represented as $10$ which is then encoded by $\ket{10}$ (Fig. 2). In general, this leads to the following encoding: $X \approx \sum_{i=-k}^{m} b_i 2^i \mapsto \ket{b_{n-1} \ldots b_{-k}}$ where $X$ is first approximated with a precision of $k+m$ significant digits and then represented by a basis vector.
\end{itemize}

\begin{figure}[h]
\centering
\includegraphics[width=0.4\textwidth]{basis_encoding.png}
\caption{Basis encoding. A number is approximated by a binary bit string (first step) and encoded by a computational basis state (second step).}
\end{figure}
**Result.** This encoding can be categorized as digital encoding because it is suitable for arithmetic computations [Leymann and Barzen 2020b]. For input numbers that are approximated by \( l \) digits, \( l \) qubits are needed for its representation. To realize this encoding, the initial \( |0\rangle \) state of qubits that represent a ‘1’ digit must be flipped into \( |1\rangle \). For one qubit, this can be done by a single operation, and thus, this encoding can be prepared in linear time.

**Related Pattern.** This pattern is a refinement of INITIALIZATION. If an algorithm requires several numbers as input, each can be encoded in BASIS ENCODING which can be processed by the QuAM pattern.

**Known Uses.** Vedral et al. [1996] give multiple examples for algorithms that perform arithmetic operations on numbers in BASIS ENCODING. A formal description of the solution above is also given in [Leymann and Barzen 2020b] and [Cortese and Braje 2018]. As only one quantum gate is needed to obtain this encoding, this state preparation routine can be implemented straightforwardly.

QuAM (Quantum Associative Memory)

Represent a collection of data elements in a quantum computer in order to perform calculations

**Context.** A quantum algorithm requires multiple numerical values \( X \) as input for further calculations.

**Solution.** Use a quantum associative memory (QuAM) to prepare a superposition of basis encoded values in the same qubit register [Leymann and Barzen 2020b]. In Fig. 3, this is illustrated for the three values \( x_1, x_2 \) and \( x_3 \) in binary format. Note that the resulting encoding is an equally weighted superposition of the basis encoded values, i.e., all amplitudes are of the same magnitude.

\[
\begin{align*}
\chi_0 & : 010 \\
\chi_1 & : 110 \\
\chi_2 & : 011
\end{align*}
\]

\[
\frac{1}{\sqrt{3}} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix} + \frac{1}{\sqrt{3}} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix}
\]

Fig. 3. Resulting Encoding. Each data value represented by a row on the left is encoded in BASIS ENCODING and an amplitude of \( \frac{1}{\sqrt{3}} \).

To load the data, the register of the quantum associative memory is in superposition of two states, a processing and a memory branch [Fig. 4]. Both branches have a load and a storage part. An additional element is first prepared into the load part of both branches (step 1). Next, the processing branch is split in such a manner, that the new element gets a proper amplitude (step 2) such that it can be stored by bringing it into superposition with the already added elements (step 3). Finally, an UNCOMPUTE cleans the both branches to be ready for the next iteration. See [Ventura and Martinez 2000] for a more detailed description of the individual steps.

**Result.** The resulting encoding is a digital encoding and therefore suitable for arithmetic computations [Leymann and Barzen 2020b]. For input \( n \) numbers that are approximated by \( l \) digits, \( l \) qubits are needed for this representation. Each of the \( n \) encoded input values is represented by a basis vector with an amplitude of \( \frac{1}{\sqrt{n}} \). All other \( 2^l - n \) amplitudes of the register are zero - in our example, \( |000\rangle, |001\rangle, |100\rangle, |101\rangle, \) and \( |111\rangle \). The amplitude vector is therefore often sparse for this encoding [Schuld and Petruccione 2018].

**Related Pattern.** This pattern refines INITIALIZATION and makes use of UNCOMPUTE. UNIFORM SUPERPOSITION creates a superposition of all computational basis states. Each of the computational basis states also represents a value in BASIS ENCODING.
**Known Uses.** The presented state preparation routine based on [Ventura and Martinez 2000] can be used whenever multiple data values need to be represented in BASIS ENCODING. Shor’s algorithm [Shor 1999] for the factorization of prime numbers, a quantum version of the Fourier transform [Coppersmith 2002], and Grover’s algorithm [Grover 1996] for unstructured search rely on this encoding. Various algorithms extend or use Grover’s algorithm and therefore also make use of this encoding.

**Amplitude Encoding**

Encode data in a compact manner that do not require calculations

**Alias.** This encoding has also been referred to as Wavefunction Encoding by [LaRose and Coyle 2020]. Every quantum system is described by its wavefunction $\psi$ which also defines the measurement probabilities. By expressing that the wavefunction is used to encode data, it is therefore implied that amplitudes of the quantum system are used to represent data values.

**Context.** A numerical input data vector $(x_0, \ldots, x_{n-1})^T$ must be encoded for an algorithm.

**Solution.** Use amplitudes to encode the data. As the squared moduli of the amplitudes of a quantum state must sum up to 1, the input vector needs to be normalized to length 1. This is illustrated in Fig. 5 for a 2-dimensional input vector that contains two data points. To associate each amplitude with a component of the input vector, the dimension of the vector must be equal to a power of two because the vector space of an $n$ qubit register has dimension $2^n$. If this is not the case, the input vector can be padded with additional zeros to increase the dimension of it. Using a suitable state preparation routine (see Known Uses), the input vector is encoded in the amplitudes of the quantum state as follows: $|\psi\rangle = \sum_{i=0}^{n-1} x_i |i\rangle$. As the amplitudes depend on the data, the process of encoding the data (but not the encoding itself) is often referred to as arbitrary state preparation.

**Result.** A data input vector of length $l$ can be represented by $\lceil \log_2(l) \rceil$ qubits - this is indeed a very compact representation. For an arbitrary state represented by $n$ qubits (which represents $2^n$ data values), it is known that at least $\frac{1}{2}2^n$ parallel operations are needed [Schuld and Petruccione 2018]. Current state preparation routines perform slightly better than $2^n$ operations [Schuld and Petruccione 2018]. However, depending on the data it may
still be possible to realize an encoding in a logarithmic runtime. For example, a UNIFORM SUPERPOSITION can be created by applying a Hadamard gate to each of the $n$ qubits - which can be done in parallel and thus in a single step. This represents a $2^n$-dimensional vector in which all data entries are $\frac{1}{\sqrt{n}}$. Similarly, sparse data vectors can also be prepared more efficiently [Schuld and Petruccione 2018].

It must be noted that if the output is also encoded in the amplitude, multiple measurements must be taken to obtain a good estimate of the output result. The number of measurements scales with the number of amplitudes - as $n$ qubits contain $2^n$ amplitudes, this is costly [Schuld and Petruccione 2018].

**Related Patterns.** This pattern refines INITIALIZATION. The encoding is more compact (in terms of qubits) than BASIS, ANGLE or QRAM ENCODING.

**Known Uses.** AMPLITUDE ENCODING is required by many quantum machine learning algorithms [LaRose and Coyle 2020]. Another example is the algorithm of Harrow, Hassidim and Lloyd [Harrow et al. 2009] (often referred to as HHL algorithm) for solving linear equations. The pre-condition that the data values can be normalized is a common assumption in machine learning [Duarte and Ståhl 2019], e.g. in support vector machine.

There are various ways to construct a state preparation routine for this encoding. For example, Plesch and Brukner [2011] and Iten et al. [2018] use the Schmidt Decomposition. For the latter, an implementation in Mathematica was presented [Iten et al. 2019]. Shende et al. [2008] presented an alternative way to construct an arbitrary quantum state which was implemented by Qiskit [Qis 2020]. PennyLane offers a loading routine for AMPLITUDE ENCODING [Pen 2020]. The library also includes an arbitrary state preparation routine that uses the algorithm proposed by Möttönen and Vartiainen [2005]. The state preparation routine by Möttönen and Vartiainen [2005] requires an exponential number of operations to encode $2^n$ data values. Q# provides functionality to compute a state preparation routine that approximates the desired amplitude encoding [QSh 2020].

4. RELATED WORK

Our patterns are based on the concept of patterns by Alexander et al. [1977] who introduced patterns for documenting best practices in the domain of buildings. Since then, the concept has been adapted by various other areas and is especially popular for the domain of software [Coplien 1996]. Leymann [2019] already presented patterns for quantum algorithms that we reviewed in Section 3. In this work, we extend the brief pattern format that was used by Leymann [2019] and present three patterns for the encoding of data. To our knowledge, no other patterns for the domain of quantum computing exist.

Perdrix [2007] introduces quantum patterns and types that are part of a formal quantum programming language. But these are not patterns in the sense of Alexander et al. [1977] as they only reflect technical details instead of describing a problem or context.

Several authors discussed the process of loading data into a quantum computer and the implications on runtime. Biamonte et al. [2017] refer to it as input problem as data can not always be loaded efficiently. Aaronson [2015] examines loading data for the HHL algorithm for solving linear equations. He points out that the logarithmic runtime...
for this algorithm can only be achieved if the Amplitude Encoding of the data can be prepared in logarithmic time. He concludes that this is a general drawback for algorithms that use this encoding, which we also emphasize in our pattern for this encoding.

Salm et al. [2020] consider given input data to support the selection of concrete quantum algorithm implementations and suitable quantum computers for execution. Thereby, they are estimating the required number of qubits and sequentially executable gates of an implementation depending on the size of the input data.

Yan et al. [2016] review different quantum representations for quantum image processing. In particular, Basis Encoding and Angle Encoding are used in various representations. They outline similarities, applications, and drawbacks of the representations but do not draw general conclusions for data encodings.

Schuld and Petruccione [2018] as well as LaRose and Coyle [2020] define various data encodings for quantum computing. We refer to these definitions in our data encoding patterns and visualize them in greater detail. LaRose and Coyle [2020] also compare data encodings in the context of classification with quantum computers. They show that in a noiseless setting, different data encodings lead to different decision boundaries that can be learned by a quantum classifier. While they discuss the findings for quantum classifier, they do not consider implications for data encodings in general. In particular, LaRose and Coyle [2020] do not consider Basis Encoding as these are not common for quantum classifiers.

Schuld and Killoran [2019] point out how data encodings and kernels in machine learning are related. They show that an input encoding (that maps a numerical input value into the high dimensional vector space of a quantum system) defines a quantum kernel. They refer to a specific encoding as a quantum feature map $\phi$ and point out that different encodings lead to different values of the inner product between the encoded data values. Very recently, there is active research about learning suitable data encodings for quantum machine learning [LaRose and Coyle 2020; Lloyd et al. 2020]. Here, we depict a more general view on encodings and do not focus on machine learning.

5. CONCLUSION AND FUTURE WORK

In this paper, we formulated three common data encoding as patterns. In order to explain ‘how’ the encoding is realized, we described and visualized it with a sketch. In the result section, we outlined consequences (required qubits, runtime of the encoding process, etc.) and thus elaborate ‘why’ a particular encoding should be chosen. We conclude that there is not ‘the’ best encoding for quantum computation addressing different problems on current devices. If arithmetic computations shall be performed, a digital encoding (e.g., Basis Encoding or QAM) may be preferred. To store as much data as possible in a small number of qubits, a compact encoding like Amplitude Encoding may be the best choice. However, it must also be taken into account that the state preparation for Amplitude Encoding is costly in terms of operations. Other encodings (e.g., Angle Encoding) exists for which state preparation can be done by only few operations, but which are not optimal in the number of required qubits.

We plan to collect more patterns for quantum computing. We will investigate other encodings mentioned in the literature [Leymann and Barzen 2020b; LaRose and Coyle 2020; Schuld and Petruccione 2018]. In addition, we are extending our pattern repository [Leymann and Barzen 2020a; Weigold et al. 2020] to support quantum computing patterns by including mathematical formulas and quantum gates. The presented encoding patterns will contribute to improve the estimation of required quantum resources for quantum algorithm implementations in the future [Salm et al. 2020].

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Data Encoding Patterns for Quantum Computing — Page 10